

Cortical-Inspired Open-Bigram Representation for Handwritten Word Recognition

Théodore Bluche, Christopher Kermorvant, Claude Touzet and Hervé Glotin

A2iA SAS, Paris, France

Teklia SAS, Paris, France

UMR CNRS NIA 7260, Aix Marseille Univ., Marseille, France

UMR CNRS LSIS 7296, AMU, Univ. Toulon, ENSAM, IUF, France

tbluche@protonmail.com, kermorvant@tekliia.com, claude.touzet@univ-amu.fr, glotin@univ-tln.fr

Abstract—Recent research in the cognitive process of reading hypothesized that we do not read words by sequentially recognizing letters, but rather by identifying open-bigrams, i.e. couple of letters that are not necessarily next to each other. In this paper, we evaluate a handwritten word recognition method based on original open-bigrams representation. We trained Long Short-Term Memory Recurrent Neural Networks (LSTM-RNNs) to predict open-bigrams rather than characters, and we show that such models are able to learn the long-range, complicated and intertwined dependencies in the input signal, necessary to the prediction. For decoding, we decomposed each word of a large vocabulary into the set of constituent bigrams, and apply a simple cosine similarity measure between this representation and the bagged RNN prediction to retrieve the vocabulary word. We compare this method to standard word recognition techniques based on sequential character recognition. Experiments are carried out on two public databases of handwritten words (Rimes and IAM). The bigram decoder results with our bigram decoder are comparable to more conventional decoding methods based on sequences of letters.

I. INTRODUCTION

Taking inspiration in Biology is sometimes very efficient. For example, deep neural networks (NN) - which are outperforming all other methods (including support vector machines, SVM) in image recognition - are based on a series of several (usually 5 to 15) neurons layers, each layer involving sparsity in the activation pattern (a biological trait of the cortical map). The analogy continues with the modeling of the cortex as a hierarchy of cortical maps. Thanks to the analysis of reaction time in cognitive psychology experiments, the minimal number of cortical maps involved in a cognitive process is estimated to about five, the same order of magnitude as the number of layers in deep neural networks for computer vision tasks. In the case of handwritten word recognition, Dehaene et al. have proposed a biologically plausible model of the cortical organization of reading [1] that assumes seven successive steps of increasing complexity, from the retinal ganglion cells to a cortical map of the orthographic word forms (Fig. 1). One of the most recent successes of experimental psychology was the demonstration that human visual word recognition uses an explicit representation of letter position order based on letter pairs: the open-bigram coding [2], [3], [4], [5], [6].

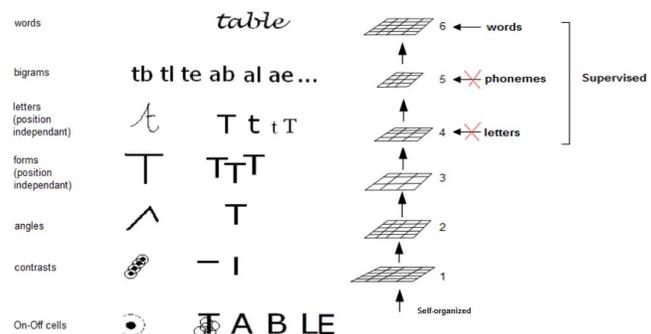


Fig. 1: The cognitive process of reading, a seven steps procedure that includes an open-bigrams representation layer. Additional information helps the organization of levels 4 and 5, when using a phonics method, but not a whole language method (today banned from reading teaching for lack of efficiency, adapted from [1] and [7]).

As demonstrated in [8], open-bigrams (OB) allow an over-coding of the orthographic form of words that facilitates recognition. OB coding favors same length words (i.e., neighbors of similar lengths). In the context of learning to read, the existence of the OB layer just before the orthographic word representation has been used to explain the lack of efficiency of whole language method (today banned from reading teaching) compared to the phonics method which explicitly supervises the organization of the OB map (with syllables), where the global method does not (Fig. 1).

Since cognitive psychology has demonstrated the existence of the OB layer, the hypothesis has been put forward [8] that the orthographic representation of words may have evolved in order to take into account the topology of the OB space, instead of the topology of the single letter space. Our goal here is to test this hypothesis, comparing OB vs sequential character recognition for word recognition. A state-of-the-art decoder based on a Long Short-Term Memory Recurrent Neural Networks (LSTM-RNN) is used on two public databases of handwritten words (Rimes and IAM).

The remaining of this paper will be divided as follows. In

Section II, we present related methods for handwritten word recognition. Then, we describe the open-bigram representation of words and the proposed decoder in Section III. The experimental setup, including the data and the bigram prediction model, is explained in Section IV. Finally, we present our results in Section V, before concluding in Section VI.

II. RELATED WORK

In this section, we give a brief overview of existing techniques for handwritten word recognition. Historically, the methods may be divided in three broad categories. The first approach is whole word recognition, where the image of the full word is directly classified into word classes, without relying on the character level (e.g. in [9], [10]). In the second method, the word image is segmented into parts of characters (strokes or graphemes). The segments are grouped and scored, and character sequences are obtained with a graph search (e.g. in [11]) or with hidden Markov models (HMMs, e.g. in [12]). The last method, most popular nowadays, is a segmentation-free approach. The goal is to predict a character sequence from the image without segmenting it first. The techniques include scanning a sliding window to extract features used in an HMM (e.g. in [13]), or to feed the image to a neural network able to output sequences of character predictions (e.g. SDNNs [14] or MDLSTM-RNN [15]).

More recently, different approaches have been proposed to recognize words using character bigrams, and therefore closer to the method we propose in this paper. [16] propose to predict both the characters and ngrams of characters with two distinct convolutional neural networks (CNNs) to recognize text in natural images. Their approach includes a conditional random field as decoder. Similarly, [17] train a CNN with a cross-entropy loss to detect common unigrams, bigrams or trigrams of characters in a handwritten word image. The output of the network is matched against the lexicon using canonical correlation analysis. [18] use Fisher vectors from images and pyramidal character histograms, to learn a feature space shared by the word images and labels, for word spotting, also using canonical correlation analysis.

III. PROPOSED METHOD

A. An Open-Bigram Representation of Words

The letter bigrams of a word w is the set of pairs of consecutive letters. The **open-bigram of order d** is the set of pairs of letters separated by d other letters in the word, which we call $\mathcal{B}_d(w)$:

$$\mathcal{B}_d(w) = \{w_i w_{i+d} : i \in \{1 \dots |w| - d\}\}. \quad (1)$$

The usual bigrams are open-bigrams of order 1. By extension, we call $\mathcal{B}_0(w)$ the set of letters in the word w . For example, for word `word`, we have:

$$\begin{aligned} \mathcal{B}_1(\text{word}) &= \{\text{or}, \text{rd}, \text{wo}\} \\ \mathcal{B}_2(\text{word}) &= \{\text{od}, \text{wr}\} \\ \mathcal{B}_3(\text{word}) &= \{\text{wd}\}. \end{aligned}$$

The general open-bigram representation of a word is the union of

$$\mathcal{B}_{d_1, \dots, d_n}(w) = \mathcal{B}_{d_1}(w) \cup \dots \cup \mathcal{B}_{d_n}(w). \quad (2)$$

For example, $\mathcal{B}_{1,2,3}(\text{word}) = \{\text{od}, \text{or}, \text{rd}, \text{wd}, \text{wo}, \text{wr}\}$.

We extend \mathcal{B} into \mathcal{B}' by including special bigrams for the letters at the beginning and end of a word:

$$\mathcal{B}'(w) = \mathcal{B}(w) \cup \{-w_0, w_{|w|}\}. \quad (3)$$

So, for example,

$$\mathcal{B}'_{1,2,3}(\text{word}) = \{-w, d_-, \text{od}, \text{or}, \text{rd}, \text{wd}, \text{wo}, \text{wr}\}. \quad (4)$$

In this paper, we will call B the set of all bigrams, and W the set of all words. We will represent a word of the vocabulary $w \in W$ as a normalized binary vector $\mathbf{v}_{w \in W} \in \mathfrak{R}^{|B|}$

$$\mathbf{v}_w = \frac{[\delta(b \in \mathcal{B}(w))]_{b \in B}}{\sqrt{|\mathcal{B}(w)|}}, \quad (5)$$

i.e. the vector with 0 everywhere and $1/\sqrt{|\mathcal{B}(w)|}$ at indices corresponding to bigrams of the word. Stacking the vector representations of all the words in the vocabulary yields the vocabulary matrix $V \in \mathfrak{R}^{|W| \times |B|}$.

Note that in this representation, the bigrams form an unordered set. We *do not know*: (i) where the bigrams are, (ii) what is the order of a given bigram, (iii) how many times it occurs. The goal is to build a word recognition decoder in the bigram space.

B. An Open-Bigram Decoder

While the trivial representation of a word is an ordered sequence of letters, the order in the bigram space is locally embedded in the bigram representation. Most state-of-the-art word recognition systems recognize sequences of letters, and organize the vocabulary for a constrained search as directed graphs, such as prefix trees, or Finite-State Transducers. On the other hand, we can interpret the bigram representation as encoding directed edges in a graph, although we will not explicitly build such a graph for decoding.

On Figure 2, we show the graph for a representation of the word into a sequence of letters. Gray edges show the potential risk of a misrecognition in the letter sequences. On Figure 2(b), we display the conceptual representation of bigrams as edges. We observe that a global order of letters can emerge from the local representation. Moreover, the constituent information of a word in the bigram space is redundant, potentially making this representation more robust to mispredictions of the optical model.

The optical model is the system which provides the predictions of bigrams from the image (or, in the classical approach sequences of character predictions). That is, it provides a confidence measure that each bigram b is present in image x : $0 \leq p_b(x) \leq 1$. This is transformed into a vector in the bigram space:

$$\mathbf{q}_x = \frac{[p_b(x)]_{b \in B}}{\sqrt{\sum_b p_b^2(x)}}. \quad (6)$$

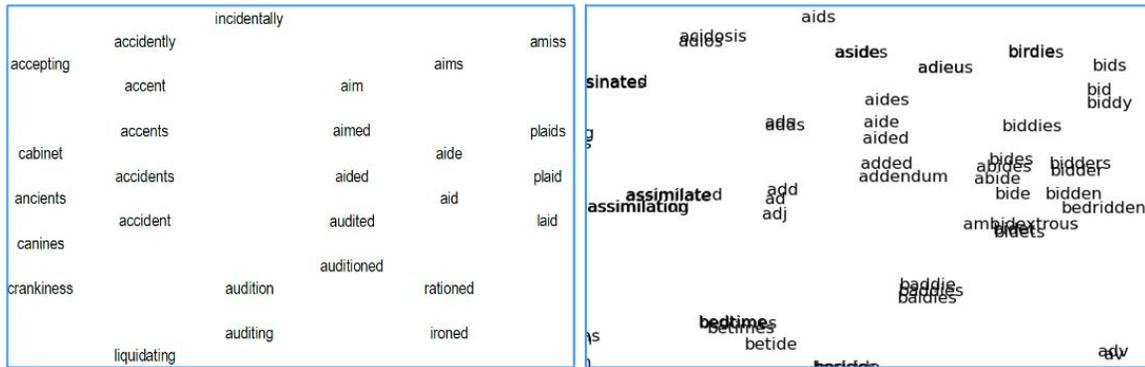


Fig. 3: Visualization of the bigram representation of the English vocabulary, for $d = 1..3$ [8] (left), vs after t-SNE [19] (right).

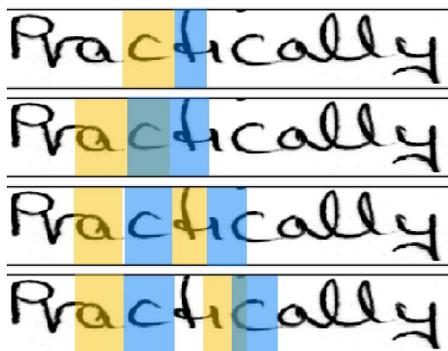


Fig. 4: Hypothetical context needed in the input image to make two consecutive (yellow and blue) bigram predictions, for $d = 0$ (left, to predict c , then t) to 3 (right, to predict ai , then cc). As d increases, the contexts become more complex to model: they involve long range dependencies and are highly intertwined.

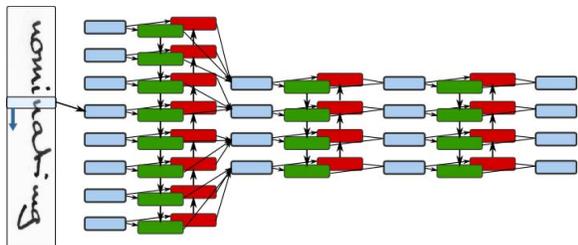


Fig. 5: Neural network architecture. A sequence of feature vectors is extracted with a sliding window, and fed to a multi-layer BLSTM network, with subsampling after the first BLSTM layer. The output is a sequence of open-bigram prediction.

The next LSTM layers have 150 units, and are connected to a feed-forward layer with 150 units. The last two LSTM layers and feed-forward layer have 200 hidden units.

The networks are trained with stochastic gradient descent to minimize the CTC criterion, i.e. the Negative Log-Likelihood

(NLL) of the correct label sequence. We set the learning rate to 0.001, and stopped the training when the NLL on the validation set did not decrease for 20 epochs, and kept the network yielding the best NLL on the validation set. These RNNs are trained to predict sequences of fixed order bigrams. Here, we are interested in a word representation as a bag of bigrams, which does not carry any information about the sequential order in which the bigrams appear, the number of times each bigram appears, or the order of each individual bigram. That is, we are interested in a decoder which considers an unordered set of bigrams predictions across bigram orders.

We **forget the temporal aspect** of bigram predictions by taking the maximum value of a given bigram prediction by the RNN (where $rnn_d(x, t)$ if the output of the RNN for order d , input image x at timestep t):

$$p_{d,b}(x) = \max_t rnn_d(x, t), \quad (10)$$

and we **forget the bigram order** by taking the maximum output across different values of d :

$$p_b(x) = \max_d \max_t rnn_d(x, t). \quad (11)$$

Predicting a sequence of bigrams of fixed order is challenging. On Figure 4, we show the hypothetical context needed to make two consecutive predictions, for bigram order $d = 0..3$. RNNs are popular for handwriting recognition, and can consider a context size of variable length – but still local – to predict characters ($d = 0$). For $d = 1$, the required context is still local (and would span two consecutive characters), but overlap, because each character is involved in two bigrams. For $d > 1$, the context is even split into two areas (covering the involved characters) that might be far apart depending on d . Contexts for different predictions are entangled: the whole area between two characters forming a bigram is not relevant for this bigram (and might be of varying size), but will be important to predict other bigrams. It means that the RNN will have to remember a character observation for some time, until it sees the second character of the bigram, while ignoring the area in between for this bigram prediction, but remembering it since it will be useful in order to predict other bigrams. The number of classes for bigrams is also 26 times larger than

the number of characters, making the classification problem harder, and the number of examples per class in training smaller.

V. RESULTS

In this paper, we focused on a subset of Rimes and IAM word databases, which makes the comparison with published results difficult. Instead, we compared the bigram decoder approach to decoding with standard models, consisting of a beam search with Viterbi algorithm in the lexicon. However, these standard models yield state-of-the-art results on the reference task for the two considered database [24].

A. Baseline Systems based on HMMs and Viterbi Decoding

We built several models and used the same vocabulary as for the bigram decoder, and no language model (all words have the same prior probability). These baseline systems are based on HMMs, with emission models made either of Gaussian mixtures (GMM/HMM), Multi-Layer Perceptrons (MLP/HMM) or Recurrent Neural Networks (rnn_0 /HMM). They are almost identical to those presented in a previous work [24], where a comparison is made with state-of-the-art systems for handwritten text line recognition.

TABLE II: Word Error Rates (%) with baseline systems and Viterbi decoding of character sequences.

	Dataset	Models		
		GMM/HMM	MLP/HMM	rnn_0 /HMM
Rimes	Valid.	37.38	14.82	10.79
<i>Viterbi (Char. seq.)</i>	Test	36.24	14.45	10.03
IAM	Valid.	27.64	11.73	10.21
<i>Viterbi (Char. seq.)</i>	Test	37.96	19.97	17.49

On Table II, we report the percentages of word errors on the validation and test sets of Rimes and IAM. The best word error rates are around 10% (17.5% on the test set of IAM), and constitute the baseline performance to which the bigram approach is to be compared.

B. Measuring the Quality of Bigram Predictions

Since we keep a confidence value for all bigrams in the prediction vector, rather than using a binary vector (cf. Eq. 6), we modified the formulation of precision and recall. A bigram $b \in \mathcal{B}(w)$ is correctly retrieved with confidence $p_b(x)$, and missed with confidence $(1 - p_b(x))$. Similarly, a bigram not in the representation $\mathcal{B}(w)$ of word w is falsely recognized with confidence $p_b(x)$, and correctly ignored with confidence $(1 - p_b(x))$. It gives us the following expressions for precision and recall

$$precision = \frac{\sum_{(x,w)} \sum_{b \in \mathcal{B}(w)} p_b(x)}{\sum_x \sum_{b' \in \mathcal{B}} p_{b'}(x)}, \quad (12)$$

$$recall = \frac{\sum_{(x,w)} \sum_{b \in \mathcal{B}(w)} p_b(x)}{\sum_{w \in \mathcal{W}} |\mathcal{B}(w)|}, \quad (13)$$

which are the usual ones when $p_b(x) \in \{0, 1\}$. The *F-measure* is calculated from precision and recall with the usual formula.

The results for all RNNs, and for the combination of orders, are reported on Table III. The precision and recall decrease

TABLE III: Precision, Recall and F-measure of OB detection by RNNs with different orders d .

	d							1,2,3	1',2',3'
	1	1'	2	2'	3	3'			
π	89.9	91.2	79.8	82.8	74.8	82.6	84.5	84.0	
ρ	87.6	89.3	84.8	85.8	83.4	80.9	86.7	88.5	
F	0.89	0.90	0.82	0.84	0.79	0.82	0.89	0.86	
π	87.3	89.3	77.7	81.6	62.3	76.2	80.5	81.0	
ρ	86.2	88.5	82.3	84.0	77.5	78.6	84.3	86.4	
F	0.87	0.89	0.80	0.83	0.69	0.77	0.82	0.84	

as the bigram order increases, which is not surprising, given that higher order bigrams are more difficult to recognize with these sequence models. We also see that including the special bigrams for word beginnings and endings generally improves the results. This is not surprising either: the RNNs are good at recognizing them. Despite this performance decrease, the precision remains above 70%, which limits the amount of noise that will be included in the bigram representation for recognition. Combining the recognition across orders, we obtain a precision of around 84% on Rimes and 80% on IAM. The recall tends to be higher than the precision, staying around or above 80% in all configurations. Across orders, the recall is above 88% on Rimes and 86% on IAM. The high recall will limit the amount of missing information in the bigram representation.

Overall, the F-measure for bigram recognition is above 80%, which is a good starting point, given that (i) the vocabulary used in decoding will add constraints and may help recovering from some mistakes in the bigram recognition, and (ii) the redundancy and order encoded in the bigram may limit the impact of misrecognitions.

C. Word Recognition using Bigram Predictions

On Table IV, we report the results of bigram decoding. For each word image in the validation and test sets, we computed the bigram predictions with the RNNs described above. We combined the different orders as explained previously, and either added the special bigrams for word boundaries and/or the single character predictions or not. We computed the cosine similarity to the bigram decomposition of all words in the vocabularies in the same representation space (*i.e.* same orders, and same choices for the inclusion of special bigrams and single characters) by computing the product of the vocabulary matrix V by the recognition vector. We counted the number of times the correct word was not the most similar one.

TABLE IV: Decoding results (% of word errors).

Decoding	Model	Rimes		IAM	
		Valid	Test	Valid	Test
<i>Viterbi (Char. seq.)</i>	Best in Table II	10.79	10.03	10.21	17.49
<i>Cosine (bigrams)</i>	$rnn_{1,2,3}$	25.58	24.37	13.45	20.82
	$rnn_{1',2',3'}$	12.43	12.27	11.80	19.25
	$rnn_{0,1,2,3}$	11.03	10.41	11.98	19.61
	$rnn_{0,1',2',3'}$	9.81	9.43	11.09	18.39

We see that adding the special bigrams for word boundaries improves the results, especially when single characters are not included in the representation. A possible explanation, besides

the fact that they tend to be recognized more easily, could be that they provide a very useful information to disambiguate words having a similar bigram representation (e.g. them and theme). Adding single characters also improves the performance of the decoder, especially when the boundary bigrams are not included in the representation. The gain obtained with the single characters is about the same – sometimes a little better – as the gain with boundaries. It might be due to the much better recognition of the RNN for single characters (precision and recall over 90%), as well as the added redundancy and complementary information provided. The best performance is achieved with both single characters and word boundaries, although the gain compared to adding only one of them is slight. The error rates are competitive (IAM) or better (Rimes) than the best error rates obtained by classical character sequence modeling and Viterbi decoding.

VI. CONCLUSION

State-of-the-art systems, as well as most of the systems for handwritten word recognition found in the literature, model words as a sequence of characters. In this paper, we have proposed a simple alternative model, inspired by the recent findings in cognitive neurosciences research on reading.

We focused on the representation of words in the open-bigram space and built an handwritten word recognition system operating in that space. We were interested in observing how a simple decoding scheme, based on a mere cosine similarity measure in the bigram space, compared to traditional methods. The main apparent difficulty arises from the fact that the global ordering of characters and the distance between bigram constituents are lost in this representation.

The qualitative results presented in the first section showed that the envisioned approach was viable. We have seen that the correct orthographic form of words can be retrieved with a limited and local knowledge of character orders. Moreover, we validated that words that are close in orthographic form are also close in the bigram space. Thus, we demonstrated that the open-bigram representation shows interesting and competitive metric properties for the word recognition.

Acknowledgments: This work was conducted in COGNILEGO project 2012-15, supported by the French Research Agency under the contract ANR 2010-CORD-013 <http://cognilego.univ-tln.fr>.

REFERENCES

- [1] S. Dehaene, L. Cohen, M. Sigman, and F. Vinckier, "The neural code for written words: a proposal," *Trends in cognitive sciences*, vol. 9, no. 7, pp. 335–341, 2005.
- [2] C. Whitney, D. Bertrand, and J. Grainger, "On coding the position of letters in words: a test of two models." *Experimental psychology*, vol. 59, no. 2, p. 109, 2012.
- [3] P. Gomez, R. Ratcliff, and M. Perea, "The overlap model: a model of letter position coding." *Psychological review*, vol. 115, no. 3, p. 577, 2008.
- [4] J. Grainger and W. Van Heuven, "Modeling letter position coding in printed word perception." *The mental lexicon*, pp. 1–24, 2003.
- [5] H. Glotin, P. Warnier, F. Dandurand, S. Dufau, B. L  t  , C. Touzet, J. Ziegler, and J. Grainger, "An adaptive resonance theory account of the implicit learning of orthographic word forms," *Journal of Physiology-Paris*, vol. 104, no. 1, pp. 19–26, 2010.
- [6] S. Dufau, "Auto-organisation des repr  sentations lexicales au cours de l'apprentissage de la lecture: approches comportementale   lectrophysiologique et neuro-computationnelle," Ph.D. dissertation, Universit   de Provence, 2008.
- [7] C. Touzet, "The Theory of neural Cognition applied to Robotics," *International Journal of Advanced Robotic Systems*, 12:74, 2015.
- [8] C. Touzet, C. Kermorvant, and H. Glotin, "A Biologically Plausible SOM Representation of the Orthographic Form of 50000 French Words," in *Advances in Self-Organizing Maps and Learning Vector Quantization, Springer AISC 295*, 2014, pp. 303–312.
- [9] C. Parris  , "Global word shape processing in off-line recognition of handwriting," *IEEE transactions on pattern analysis and machine intelligence*, vol. 18, no. 4, pp. 460–464, 1996.
- [10] S. Madhvanath and V. Govindaraju, "Holistic lexicon reduction for handwritten word recognition," in *Electronic Imaging: Science & Technology*. International Society for Optics and Photonics, 1996, pp. 224–234.
- [11] Y. Bengio, Y. LeCun, C. Nohl, and C. Burges, "Lerec: A NN/HMM hybrid for on-line handwriting recognition," *Neural Computation*, vol. 7, no. 6, pp. 1289–1303, 1995.
- [12] S. Knerer, E. Augustin, O. Baret, and D. Price, "Hidden Markov model based word recognition and its application to legal amount reading on French checks," *Computer Vision and Image Understanding*, vol. 70, no. 3, pp. 404–419, 1998.
- [13] A. Kaltenmeier, T. Caesar, J. M. Gloger, and E. Mandler, "Sophisticated topology of hidden Markov models for cursive script recognition," in *Document Analysis and Recognition, 1993., Proceedings of the Second International Conference on*. IEEE, 1993, pp. 139–142.
- [14] Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, "Gradient-based learning applied to document recognition," *Proceedings of the IEEE*, vol. 86, no. 11, pp. 2278–2324, 1998.
- [15] A. Graves and J. Schmidhuber, "Offline handwriting recognition with multidimensional recurrent neural networks," in *Advances in Neural Information Processing Systems*, 2009, pp. 545–552.
- [16] M. Jaderberg, K. Simonyan, A. Vedaldi, and A. Zisserman, "Deep structured output learning for unconstrained text recognition," *CoRR*, vol. abs/1412.5903, 2014. [Online]. Available: <http://arxiv.org/abs/1412.5903>
- [17] A. Poznanski and L. Wolf, "Cnn-n-gram for handwriting word recognition," in *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, 2016, pp. 2305–2314.
- [18] J. Almaz  n, A. Gordo, A. Forn  s, and E. Valveny, "Word spotting and recognition with embedded attributes," *IEEE transactions on pattern analysis and machine intelligence*, vol. 36, no. 12, pp. 2552–2566, 2014.
- [19] L. Van der Maaten and G. Hinton, "Visualizing data using t-SNE," *Journal of Machine Learning Research*, vol. 9, no. 2579–2605, p. 85, 2008.
- [20] E. Augustin, M. Carr  , E. Grosicki, J.-M. Brodin, E. Geoffrois, and F. Preteux, "RIMES evaluation campaign for handwritten mail processing," in *Proceedings of the Workshop on Frontiers in Handwriting Recognition*, no. 1, 2006.
- [21] U.-V. Marti and H. Bunke, "The IAM-database: an English sentence database for offline handwriting recognition," *International Journal on Document Analysis and Recognition*, vol. 5, no. 1, pp. 39–46, Nov. 2002.
- [22] R. Buse, Z. Q. Liu, and T. Caelli, "A structural and relational approach to handwritten word recognition." *IEEE Transactions on Systems, Man and Cybernetics*, vol. 27, no. 5, pp. 847–61, Jan. 1997. [Online]. Available: <http://www.ncbi.nlm.nih.gov/pubmed/18263093>
- [23] A.-L. Bianne, F. Menasri, R. Al-Hajj, C. Mokbel, C. Kermorvant, and L. Likforman-Sulem, "Dynamic and Contextual Information in HMM modeling for Handwriting Recognition," *IEEE Trans. on Pattern Analysis and Machine Intelligence*, vol. 33, no. 10, pp. 2066 – 2080, 2011.
- [24] T. Bluche, H. Ney, and C. Kermorvant, "A Comparison of Sequence-Trained Deep Neural Networks and Recurrent Neural Networks Optical Modeling for Handwriting Recognition," in *International Conference on Statistical Language and Speech Processing*, 2014, pp. 199–210.
- [25] K. Atkinson, "GNU Aspell." [Online]. Available: <http://aspell.net/>
- [26] A. Graves, S. Fern  ndez, F. Gomez, and J. Schmidhuber, "Connectionist temporal classification: labelling unsegmented sequence data with recurrent neural networks," in *International Conference on Machine learning*, 2006, pp. 369–376.